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- Separated (unmixed) contributor genotypes
- Rapid calculation from prior and posterior
- Extreme set contains the matching genotype
- In set: LR of evidence ≥ matching genotype
- Smallest RMP sum containing matching genotype
- Singleton set reduces to ordinary RMP
- Chance of false positive for innocent person









Combine independent tests $log(LR) = log(LR_1 \times ... \times LR_L)$ $= log(LR_1) + ... + log(LR_L)$ Distribution of independent sums is the convolution of their distributions

Fast calculation









Case example

A homeless man took a woman into an alleyway and sexually assaulted her. He stole her phone so she couldn't call for help.

He threatened her, saying, "Don't tell anyone about this or I will kill you" and "You are never going to see your mother again."

Fearing for her life, she followed him across a bridge and into a downtown Pittsburgh park. He sexually assaulted her again, but she screamed and ran toward a hotel.

Hotel workers came to her aid, and chased after him. Police officers caught him a few blocks away.

Crime lab DNA analysis

The Allegheny County Medical Examiner's Office developed informative DNA data from the evidence.

Using limited DNA mixture interpretation methods, the lab said that no conclusion can be made due to insufficient data on some items, and the complexity of the data on others.

They did not report DNA match statistics.

	log(LR)	
Description	Victim	Suspect
non-sperm rectal swabs	16.06	25.81
sperm rectal swabs		3.69
right hand fingernails	30.72	21.31
left hand fingernails	29.97	16.30

LR values range from thousands to nonillions





















Error statement (RMP)

Question What is the chance that someone who didn't contribute their DNA to the rectal swabs has an LR of at least 4.89 thousand?

Answer One in 28.7 million for an (ethnic group) person.

Related RMP methods

- approximate the LR distribution
- Monte Carlo simulation for LR tail
- branch and bound for small sets
- divide and conquer for larger sets
- don't report any error measure
- give generic RMP ≤ 1/LR bound

RMP much less than 1/LR rmp = csum/alr = (1/lr)*(lr/alr)*csum = (1/4893)*(1/2.400)*(1/2448) = (1/4893)*(1/5873) = 1/28736000 alr average LR on NCD tail csum sum over right CD tail lr likelihood ratio

Statistics & Law

- RMP as probability of observing misleading statistical evidence
- Evidence & uncertainty are different
- LR for evidence, RMP for uncertainty
- Initial presumption of innocence (null hypothesis), defendant not contributor
- More evidence increases LR
- RMP as "p-value" for false positives
- Reduce error beyond reasonable doubt

Conclusions

• LR summarizes DNA evidence • RMP gives the error probability

RMP x population size = number of innocent people with DNA evidence as strong as for defendant

> LR (evidence) & RMP (error) both help the trier of fact understand DNA evidence

